

Contribution from the Department of Inorganic Chemistry,  
University of Umeå, S-901 87 Umeå, Sweden**Equilibrium and Structural Studies of Silicon(IV) and Aluminum(III) in Aqueous Solution. 21. A Potentiometric and  $^{27}\text{Al}$  NMR Study of the System  $\text{H}^+ - \text{Al}^{3+} - \text{MoO}_4^{2-}$** 

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Equilibria in the  $\text{H}^+ - \text{Al}^{3+} - \text{MoO}_4^{2-}$  system have been studied by potentiometry and  $^{27}\text{Al}$  NMR spectroscopy in 0.6 M Na(Cl) medium at 25 °C. The total concentration of aluminum,  $B$ , and molybdate,  $C$ , were varied within the limits  $0.9 \leq B/\text{mM} \leq 10$ ,  $5.5 \leq C/\text{mM} \leq 120$ , and  $2 \leq C/B \leq 12$  within the range  $1.5 \leq -\log [\text{H}^+] \leq 6.0$ . All data unambiguously show that one single ternary species,  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$ , is formed. According to potentiometric data, the formation constant for this species (as related to the reaction  $6\text{H}^+ + \text{Al}^{3+} + 6\text{MoO}_4^{2-} \rightleftharpoons \text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$ ) is  $\log (\beta_{6,1,6} \pm 3\sigma) = 50.95 \pm 0.04$ . Independent  $^{27}\text{Al}$  NMR data yielded the value  $50.96 \pm 0.06$ , i.e. in full agreement with emf data. The high thermodynamic stability of the complex was manifested in a model calculation, showing that even at  $B = 10^{-5}$  M,  $C = 6 \times 10^{-5}$  M, and  $-\log [\text{H}^+] = 3.7$ , 40% of  $B$  and  $C$  remained bound in this species. In acidic media, equilibration times of approximately 6 h were observed, while in near-neutral solutions the decomposition rate is higher by several orders of magnitude. With  $-\log [\text{H}^+] \leq 2$ , the complex decomposes with the formation of free aluminum ions and isopoly molybdates, while in near-neutral solutions ( $-\log [\text{H}^+] \geq 5$ ) the decomposition yields amorphous aluminum hydroxide and molybdate ions. The solubility product for this phase, defined by the reaction  $\text{Al}^{3+} + 3\text{H}_2\text{O} \rightleftharpoons \text{Al}(\text{OH})_3(\text{s}) + 3\text{H}^+$ , was determined to be  $\log (K_{-3,1,0} \pm 3\sigma) = -10.49 \pm 0.08$ . Data were analyzed with the computer programs LETAGROPVRID and SOLGASWATER.

**Introduction**

In two current research projects in this department, speciation and equilibria in systems containing  $\text{Al}(\text{III})^1$  and  $\text{Mo}(\text{VI})^2$  are being investigated. The title system might therefore be regarded as a link between these projects.

Literature information concerning equilibria in the system  $\text{H}^+ - \text{Al}^{3+} - \text{MoO}_4^{2-}$  is quite confusing. Thus, thermodynamic data available in ref 3 and 4 seem to indicate that a species containing six molybdenum atoms per aluminum atom is formed. However, the reported charge for this species ranges from  $-3$  to  $-9$ , and equilibrium constants differing by 15 orders of magnitude have been reported.

On the other hand, according to the comprehensive review on heteropoly and isopoly oxymetalates given by Pope,<sup>5</sup> the occurrence of an aqueous complex  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$  is well established. On the basis of an assumed resemblance with the compound  $\text{Na}_3(\text{CrMo}_6\text{O}_{24}\text{H}_6) \cdot 8\text{H}_2\text{O}$ ,<sup>6</sup> even the structure for this species was postulated<sup>7</sup> to be of the so-called "Anderson" type, given in Figure 1. In the literature,  $^{27}\text{Al}$ <sup>8</sup> and  $^{17}\text{O}$  NMR<sup>9</sup> characteristics for this species have also been reported.

Whether or not this species is the only heteropoly anion formed in the title system as a function of aluminum/molybdenum ratio and pH has never been investigated. Neither have any true stability constants for the species formed been reported. For such an investigation to be successful, a necessary prerequisite is that the binary subsystems  $\text{H}^+ - \text{Al}^{3+}$  and  $\text{H}^+ - \text{MoO}_4^{2-}$  are well characterized. As such data, valid in 0.6 M Na(Cl) medium, recently have been determined within our research projects,<sup>10,11</sup> it was decided to undertake this investigation. The unbiased interpretation of data will be based on precise potentiometric titration as well as on quantitative  $^{27}\text{Al}$  NMR data.

**Table I.** Binary Species in the System  $\text{H}^+ - \text{Al}^{3+} - \text{MoO}_4^{2-}$ <sup>a</sup>

proposed formula <sup>b</sup>	( <i>p,q,r</i> )	log $\beta_{p,q,r}$	proposed formula <sup>c</sup>	( <i>p,q,r</i> )	log $\beta_{p,q,r}$
$\text{Al}^{3+}$	(0,1,0)		$\text{MoO}_4^{2-}$	(0,0,1)	
$\text{Al}(\text{OH})^{2+}$	(-1,1,0)	-5.52	$\text{HMoO}_4^-$	(1,0,1)	3.39
$\text{Al}(\text{OH})_2^+$	(-2,1,0)	-11.3	$\text{H}_2\text{MoO}_4$	(2,0,1)	7.35
$\text{Al}(\text{OH})_3$	(-3,1,0)	-17.3	$\text{Mo}_7\text{O}_{24}^{6-}$	(8,0,7)	52.42
$\text{Al}(\text{OH})_4^-$	(-4,1,0)	-23.46	$\text{HMo}_7\text{O}_{24}^{5-}$	(9,0,7)	57.23
$\text{Al}_3(\text{OH})_4^{5+}$	(-4,3,0)	-13.57	$\text{H}_2\text{Mo}_7\text{O}_{24}^{4-}$	(10,0,7)	60.78
$\text{Al}_{13}\text{O}_4(\text{OH})_{24}^{7+}$	(-32,13,0)	-109.2	$\text{Mo}_8\text{O}_{26}^{4-}$	(12,0,8)	71.62
			$\text{HMo}_8\text{O}_{26}^{3-}$	(13,0,8)	73.38
			$\text{H}_3\text{Mo}_8\text{O}_{26}^{6-}$	(15,0,8)	76.34

<sup>a</sup>(*p,q,r*) notations and formation constants are related to the reaction  $p\text{H}^+ + q\text{Al}^{3+} + r\text{MoO}_4^{2-} \rightleftharpoons \text{H}_p\text{Al}_q(\text{MoO}_4)_r^{p+3q-r}$ . <sup>b</sup>Reference 10. <sup>c</sup>Reference 11.

**Experimental Section**

**Solutions and Analysis.** Stock solutions of sodium molybdate were prepared from  $\text{Na}_2\text{MoO}_4 \cdot 2\text{H}_2\text{O}$  (Merck p.a.) and analyzed through potentiometric titrations, considering the hydrolysis model in Table I as known. The titrated values were within 0.3% of those expected from the weighings. The preparation and analysis of other solutions is described in ref 12.

**Apparatus.** The automatic system for precise emf titrations, the thermostat, and the cell arrangement are fully described elsewhere.<sup>12</sup> The calibration of the glass electrode was performed separately in solutions of known hydrogen ion concentration before and after each titration. The  $^{27}\text{Al}$  NMR spectra were measured on a Bruker WM-250 spectrometer equipped with a 10-mm multinuclear probehead. X-ray powder diffractograms of solids precipitating in near-neutral solutions were recorded on a Rigaku/"Geigerflex"D/MAXIIA diffractometer using  $\text{Cu K}\alpha$  radiation.

**Temperature and Medium.** The present investigation was carried out at  $25.00 \pm 0.05$  °C in a constant ionic medium of 0.6 M Na(Cl).

**Methods.** The potentiometric measurements were carried out as a series of titrations at a constant ratio of the total concentration of aluminum,  $B$ , and molybdate,  $C$ . The titration procedures have been described earlier in this series.<sup>12</sup> The equilibration time between titrant additions was adapted so that stable emf readings, remaining constant to  $\pm 0.02$  mV for hours, were recorded. In the present system, it was found that equilibration times of up to 6 h were needed. The reversibility of equilibria were tested by performing titrations in acidic as well as in alkaline directions.

The  $^{27}\text{Al}$  NMR measurements were carried out on batch solutions equilibrated for at least 24 h. The short spin-lattice relaxation times for the quadrupolar nucleus  $^{27}\text{Al}$  and the high stability of the spectrometer made it possible to collect data without  $\text{D}_2\text{O}$  lock of the instrument. Spectra were recorded using 8K data over a frequency domain of 2500

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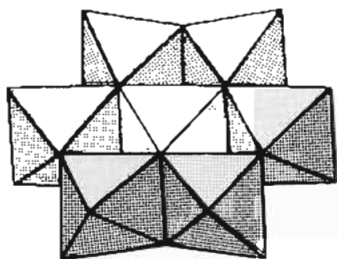


Figure 1. View of the "Anderson" structure drawn as linked octahedra.

Hz. For a spectrum, 1024 transients were collected, and an exponential line-broadening function of 0.5 Hz was applied in order to improve the signal to noise ratio. By calibration of the instrument versus a 0.0100 M  $\text{Al}^{3+}$  solution at  $-\log [\text{H}^+] = 2$  and operation of it in the absolute intensity mode, quantitative information about the concentration of each species was determined. This sample was also used as an external chemical shift standard, by using the high-frequency-positive convention.

**Data Treatment.** The equilibria under consideration in the present study can be divided into three groups as follows: (1) hydrolysis of  $\text{Al}^{3+}$ , (2) hydrolysis of  $\text{MoO}_4^{2-}$ , and (3) formation of three-component complexes according to the general reaction  $p\text{H}^+ + q\text{Al}^{3+} + r\text{MoO}_4^{2-} \rightleftharpoons \text{H}_p\text{Al}_q(\text{MoO}_4)_r^{3q-2r}$ .

In earlier parts of our research projects, formation constants for dominating hydrolytic species of  $\text{Al}(\text{III})^{10}$  and  $\text{Mo}(\text{VI})^{11}$  have been determined. These constants are given in Table I. In the evaluation of three-component data, these binary complex models were considered as known, and all effects above this level were treated as being caused by three-component species.

**Computer Programs.** The mathematical analysis of emf data in homogeneous solutions was performed with the least-squares program LETAGROPVRI, version ETTR.<sup>14,15</sup> In these computations, the error squares sum  $U = \sum (H_{\text{calcd}} - H_{\text{expt}})^2$ , where  $H$  is the analytical proton concentration with  $\text{H}_2\text{O}$ ,  $\text{Al}^{3+}$ ,  $\text{MoO}_4^{2-}$  as zero level, was minimized. The analysis of NMR data and emf data in the presence of aluminum hydroxide was performed by using the modeling computer program SOLGASWATER.<sup>16</sup>  $U = f(\log \beta)$  curves were constructed through a stepwise variation of  $\log \beta$ , and the minimum value in  $U$  was evaluated manually. In these cases, the minimized functions were  $\sum ((F_{\text{Al}^{3+}})_{\text{calcd}} - (F_{\text{Al}^{3+}})_{\text{expt}})^2$  ( $F_{\text{Al}^{3+}}$  stands for the fraction of the species  $\text{Al}^{3+}$ ) and  $\sum ((-\log [\text{H}^+])_{\text{calcd}} - (-\log [\text{H}^+])_{\text{expt}})^2$ , respectively. All standard deviations reported are defined according to Sillén.<sup>17,18</sup>

The program SOLGASWATER was also used for the construction of distribution, predominance area, and solubility diagrams. The computations were all performed on a CD Cyber 850 computer.

### Data, Calculations, and Results

Before a successful attack on a ternary system can be made, a thorough knowledge about the binary subsystems underlying it is a necessity. In the present case, these systems show quite divergent qualities. Thus, while the  $\text{H}^+ - \text{Al}^{3+}$  system becomes increasingly complicated in near-neutral solutions, the  $\text{H}^+ - \text{MoO}_4^{2-}$  system exhibits its most complicated behavior in strongly acidic solutions. The present investigation was therefore started by a series of  $^{27}\text{Al}$  NMR measurements on solutions of intermediate acidity ( $-\log [\text{H}^+] = 3.0$ ) containing  $10.0 \times 10^{-3}$  M  $\text{Al}(\text{III})$  and variable concentrations of  $\text{Mo}(\text{VI})$ . The result of these measurements is illustrated in Figure 2 and shows that, as the molybdenum concentration increases, the peak corresponding to  $\text{Al}^{3+}$  ( $\delta = 0$  ppm;  $\gamma_{1/2} = 4$  Hz) is successively replaced by a second  $\text{Al}(\text{III})$  peak ( $\delta = 15.5$  ppm;  $\gamma_{1/2} = 55$  Hz) and that this peak corresponds to a species with a  $C/B$  ratio of 6. It can also be concluded that, at this  $-\log [\text{H}^+]$  value, no species of any other  $C/B$  ratio is formed. Finally, as this plot shows that the species is formed in near-stoichiometric amounts, it can be concluded that its equilibrium constant is hard to evaluate at this  $-\log [\text{H}^+]$ .

To investigate whether complexes of different stoichiometries were formed at other  $-\log [\text{H}^+]$  values, two series of solutions at

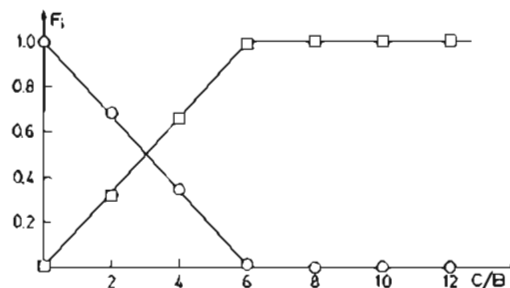


Figure 2. Fraction of  $\text{Al}(\text{III})$  found as  $\text{Al}^{3+}$  (O) and " $\text{AlMo}_6$ " (□) as a function of  $C/B$  at  $B = 10.0 \times 10^{-3}$  M and  $-\log [\text{H}^+] = 3.0$ . The curves were calculated by using the final equilibrium model.

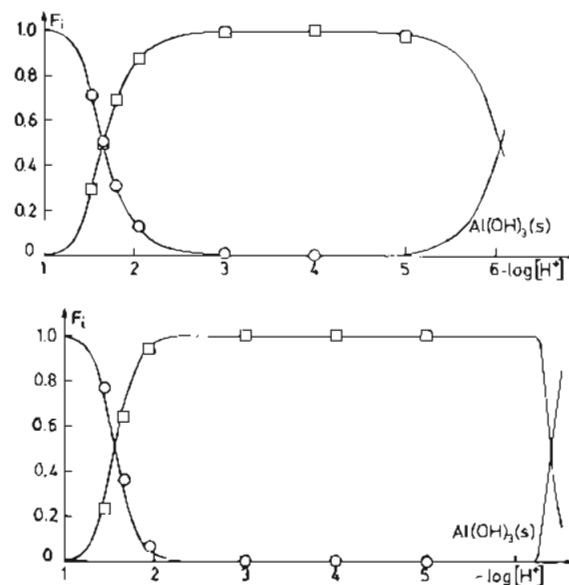


Figure 3. Fraction of  $\text{Al}(\text{III})$  in  $\text{Al}^{3+}$  (O) and " $\text{AlMo}_6$ " (□) as a function of  $-\log [\text{H}^+]$  at  $B = 10.0 \times 10^{-3}$  M and  $C =$  (a, top)  $60.0 \times 10^{-3}$  M or (b, bottom)  $120 \times 10^{-3}$  M. The curves represent the final equilibrium model.

$C/B = 6$  and 12 ( $B = 10.0 \times 10^{-3}$  M) were prepared and measured by  $^{27}\text{Al}$  NMR. The results of these measurements are illustrated in Figure 3 and show that in neither case can any "new" peak be observed. Furthermore, as the chemical shift and the line width for the peak corresponding to the " $\text{AlMo}_6$ " species remained constant throughout, a strong indication for a constant degree of protonation in this species was obtained. These figures, however, also illustrate that the complex is decomposed in solutions of high and low acidities. At low acidities, this decomposition was connected to the formation of a white precipitate, presumably aluminum hydroxide. It was therefore concluded that the stability of this ternary species preferably should be determined in solutions of high acidities.

For this reason, potentiometric titrations at  $C/B = 6$ ;  $0.9 \leq B/\text{mM} \leq 10$  and  $1.5 \leq -\log [\text{H}^+] \leq 5$  were performed. These titrations were run in the acidic as well as in the alkaline direction, and it was found that equilibration times of 6 h were needed. A total of 48 equilibrium data were collected. As NMR data had clearly indicated the presence of a species with a  $C/B$  ratio of 6, the computational work to evaluate the full stoichiometry and stability of this complex was highly simplified; i.e., only the number of protons attached and the multiplicity had to be considered.

These computations were made by using the LETAGROP<sup>13</sup> program, and the complex resulting in the lowest error squares sum  $U$  was considered the "best". From the results obtained ( $(p, q, r)$ ,  $\log (\beta \pm 3\sigma)$ ,  $U$ ,  $\sigma(H/M)$ ): (5,1,6),  $48.6 \pm 0.4$ , 765, 0.0040; (6,1,6),  $50.95 \pm 0.04$ , 5.8, 0.0003; (7,1,6),  $53.9 \pm 0.6$ , 558, 0.0034; (12,2,12),  $104.1 \pm 0.15$ , 22.5, 0.0007), it was concluded that the ternary species had the composition  $\text{H}_6\text{Al}(\text{MoO}_4)_6^{3-}$ . An independent validation of this equilibrium constant was also obtained

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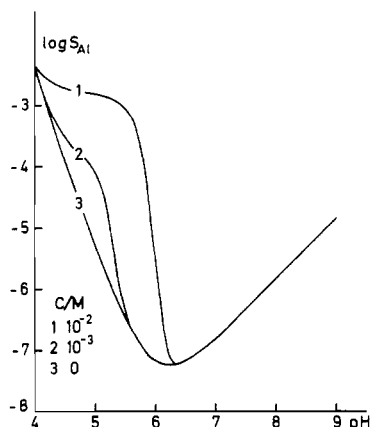
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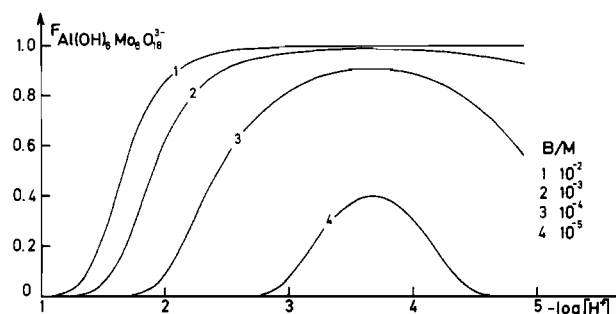


**Figure 7.** Solubility of gibbsite expressed as  $\log S_{\text{Al}}$  versus  $-\log [\text{H}^+]$  for different total concentrations of Mo(VI),  $C$ .

behave fully nonacidic; i.e. when  $-\log [\text{H}^+]$  is increased, the complex decomposes with the formation of  $\text{Al}(\text{OH})_3(\text{s})$  and  $\text{MoO}_4^{2-}$  without signs of deprotonation.

The formation of  $\text{Al}(\text{OH})_3(\text{s})$  from an aqueous solution is normally an extremely slow process. One of the reasons for this behavior is the formation of metastable polynuclear hydrolysis products in the aqueous phase. Due to the complex-forming ability of the molybdate ions, this supersaturation never occurs in the present system. Therefore, it was possible to collect reasonably stable emf data ( $dE/dt \leq 0.05$  mV/h) in the presence of this solid. From X-ray powder diffractograms, but also from the solubility product evaluated,  $\log *K_{\text{so}} = 10.49$ , the amorphous nature of this phase was demonstrated. The slow drift in emf potentials registered can probably be attributed to a slow rearrangement of the solid into a more crystalline form of aluminum hydroxide.

In the present study, attempts were also made to evaluate kinetic acid-base qualities for the species  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$ . The idea was to test whether the deprotonation rate of this species exceeded its decomposition rate. A flow system, by which steady  $-\log [\text{H}^+]$  values could be recorded 0.3–0.5 s after mixing, was constructed. At low neutralization degrees, data indicated an average  $\text{p}K_{\text{a}}$  of 6.2 for these protons, but at the same time, data collected at higher degrees of neutralization indicated a simultaneous formation of  $\text{Al}(\text{OH})_3(\text{s})$  and/or  $\text{Al}(\text{OH})_4^-$ . It was therefore concluded that data collected were nondecisive but that they definitely showed the decomposition rate of  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$  to be several orders of magnitude higher in near-neutral solutions than in acidic solutions. It can therefore be concluded that the protons surrounding the  $\text{AlMo}_6$  moiety are vital parts for stabilizing the complex.



**Figure 8.** Fraction of aluminum in the form of  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$  at  $C/B = 6$  as a function of total concentrations and  $-\log [\text{H}^+]$ .

To illustrate the thermodynamic stability of the species  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$ , a series of model calculations using the program SOLGASWATER<sup>16</sup> were performed. In the first series of calculations, the potential ability of molybdate ions to raise the solubility of gibbsite,  $\log *K_{\text{so}} = 9.60$ ,<sup>19</sup> was examined. These calculations, illustrated in Figure 7, showed that the main influence can be expected to occur at  $-\log [\text{H}^+] = 4$ –6 but also that the molybdate concentration has to exceed  $\approx 0.3 \times 10^{-3}$  M to result in any significant solubilization. Compared to that of other substances previously investigated within this series, the complexation ability of molybdate ions thus shows their closest resemblance to phthalate ions.<sup>20</sup>

In a second series of calculations, the fraction of aluminum in the form of  $\text{Al}(\text{OH})_6\text{Mo}_6\text{O}_{18}^{3-}$  was calculated at  $C/B = 6$  as a function of total concentration and  $-\log [\text{H}^+]$ . These calculations are illustrated in Figure 8 and show that still at a very high dilution ( $B = 10^{-5}$  M;  $C = 6 \times 10^{-5}$  M) approximately 40% of  $B$  and  $C$  remain bound in the ternary species at  $-\log [\text{H}^+] = 3.7$ . As, however, this complex decomposes (predominantly into  $\text{Al}^{3+}$  and  $\text{MoO}_4^{2-}$ ) at  $-\log [\text{H}^+]$  values slightly above 4, the negligible solubilization effect of low molybdate concentrations indicated above can also be understood.

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